

Formal Verification of a Three-stage Pipeline in the COSMA Environment¹

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Abstract. The case study analyzed in the paper illustrates the example of model checking in the COSMA environment. The system itself is a three-stage pipeline consisting of mutually concurrent modules which also compete for a shared resource. System components are specified in terms of Concurrent State Machines (CSM). The paper shows verification of behavioral properties, model reduction technique, analysis of counter-example and checking of real time properties.

1 Introduction

In [1] we have described the functional model of a system for processing of consecutive portions of data (or messages) submitted to its input. Each message goes through the three stages of processing which is reflected in the system's structure (Fig. 1). The system is a three-stage pipeline consisting of three modules that operate concurrently and asynchronously, in a sense that there is no general, common synchronizing process or mechanism. Moreover, two out of three modules compete for the access to the common resource, which is accessed also by some other (unspecified) agents from the system's environment. This calls for the verification if the cooperation among system components is *correct*. Indeed, due to potential coordination errors system can get deadlocked, messages can be lost or duplicated etc.

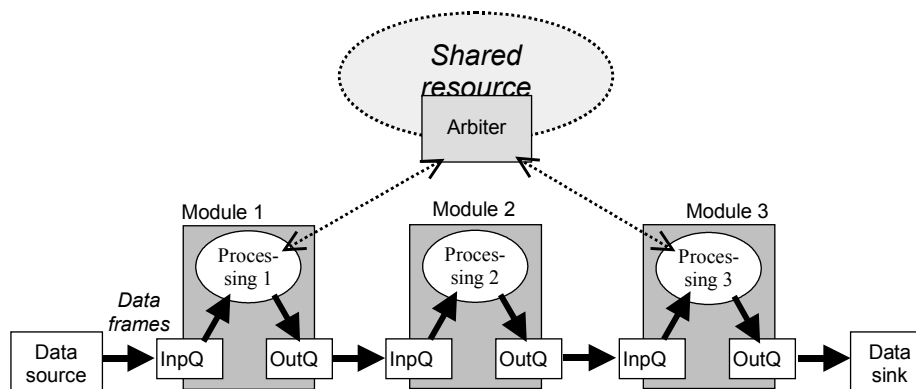


Fig. 1. Flow of data in a three-module pipeline with a shared resource

It is known that in the case of asynchronous and concurrent systems such errors are extremely hard to discover, identify and correct using typical debugging and testing procedures. Therefore, we have applied a formal procedure of *model checking* [2, 3, 4, 5], using the software tool called COSMA [6], implemented in the Institute of Computer Science, Warsaw University of Technology.

Model checking is based on the following principle. Given the finite state model M of system's behavior and property (requirement) p to be checked, one has to check if p holds for M . Usually, there is a set of techniques and algorithms (making together the model-checking environment or tool) designed for this purpose. This is

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designer's job to formulate properties to be evaluated: usually the verification involves a set of model checking experiments with several properties p_i . Additionally, if the given property does not hold for M , then so-called counterexample is provided which allows to identify the sequence of states (or events) that results in this negative evaluation. This helps to identify and correct the cause of an error.

The main limitation the model checking faces is the *exponential explosion* of model's state space size along with the increase of the number of finite state system components and their individual state spaces. So, an extensive research is being done on various techniques that can help to manage the problem. First, multiple forms of *reduction* of state space are proposed, aimed to remove the states and transitions which are irrelevant w.r.t. the evaluation of a given formula. The other approach is to calculate the state space just during the evaluation, as one can expect that in order to obtain the outcome of the evaluation only the *bounded model* will do. Still other technique consists in *compositional model checking*, where some individual parts of a system (of more acceptable size) are subject to an exhaustive state space search while the conclusion as to the behavior of a whole system is reached by some logical reasoning. Unfortunately, most of ideas of reduction found in the literature (e.g. [7, 8]) usually cannot be applied for Concurrent State Machines. This model admits *coincident* execution of actions rather than their interleaving, while most finite state models assume just the interleaved executions. Also, other known forms of reduction (e.g. *slicing* and *abstraction* [9, 10, 11]) make the use of specific properties of programs and can not be applied directly to more abstract CSM models.

In this paper we briefly describe three techniques used in a COSMA-style methodology of system's verification. First, we will analyze the system behavior step-by-step, using so-called multi-phase reduction [12, 13] which exploits some compositional features of the CSM model [14]. As a result, the system which (as naively estimated) may have as much as $4 \cdot 10^{14}$ states is finally reduced to a model of 323 states and 1406 edges, easily representable and algorithmically checkable in a split second. Then, as some properties proved to be evaluated to *false*, we illustrate how the counterexample can be obtained and analyzed. Finally, using timed version of the model, we present how real time dependencies may be analyzed. This part of the COSMA environment is under development.

2 Two-phase procedure of obtaining the reduced reachability graph

Let us recall the basic facts about the CSM model of a pipeline, described in more details in [1]. It consists of three complex modules and three individual components (data source, data sink and the arbiter) common to the whole system. Each module can be internally subdivided into six components (see also left-hand part of Fig. 2 below). In total, this makes a set of 21 cooperating components. For each of them, a separate (finite state) CSM model has been developed, aimed to specify its behavior as well as the communication to/from its communication partners. The goal was to obtain the large system's behavioral model or a graph of reachable system states, containing all the reachable states and possible execution paths among them. Then, some temporal formulas representing desirable behavioral properties of the system have been evaluated (*true* or *false*).

In [1] the emphasis was put on the specification of components and temporal properties, while the technique of obtaining the product of all the components was not analyzed. Now we proceed to the method of determining the system's behavioral model that can (to an extent) help to cope with problems of the graph size. The main idea is devoted to is the following. In order to obtain system behavioral model, one has to perform the product (\otimes) of CSM models of system components. This operation is associative and commutative. Associativity supports the important compositional property. Now, if we have - for instance - system $Z = \{m, n, p\}$ of three components, then (due to the associativity) we can obtain the behavioral model either immediately, as a 'flat' product $\otimes Z = m \otimes n \otimes p$ or in two steps: first computing the local product of some subsystem e.g. $r = m \otimes n$, then $\otimes Z = r \otimes p$. Meanwhile, before the second, final product is obtained, we can apply some reduction procedure to the partial product r . While the associativity of the product applies to other finite state models as well, this reduction makes the use of intrinsic features of CSM model itself. If machines m and n do communicate intensively with each other - it may result in a considerable reduction of a total computational effort, necessary for the computation of $\otimes Z$.

Below, we show how this general rule apply to our system of 21 components, briefly recalled above. We will proceed in the two steps or *phases*.

Generally, each phase consists in the selection of some subsystem, obtaining its CSM product and removing the *irrelevant* states and edges from it. However, one has to decide first which elements of the model are *relevant* ones and therefore have to be preserved. Relevant - in this sense - are the selected *output symbols* (produced by individual system components) and thus also the system states in which these symbols are generated. Typically, among relevant symbols are:

1. symbols that are referred to in the temporal formulas to be evaluated,

2. symbols that should be preserved for designer's convenience, e.g. because they serve as a type of markers that make the complex behavior more readable,
3. symbols that are necessary from the viewpoint of the communication among the currently reduced subsystem and remaining components².

The former two groups of symbols are decided upon by the designer while the latter one is determined by the specification of system components. Assume that in our case the relevant symbols of the types 1 and 2 above are the following ones:

msg_1, msg_4, doProc_1, doProc_2, doProc_3

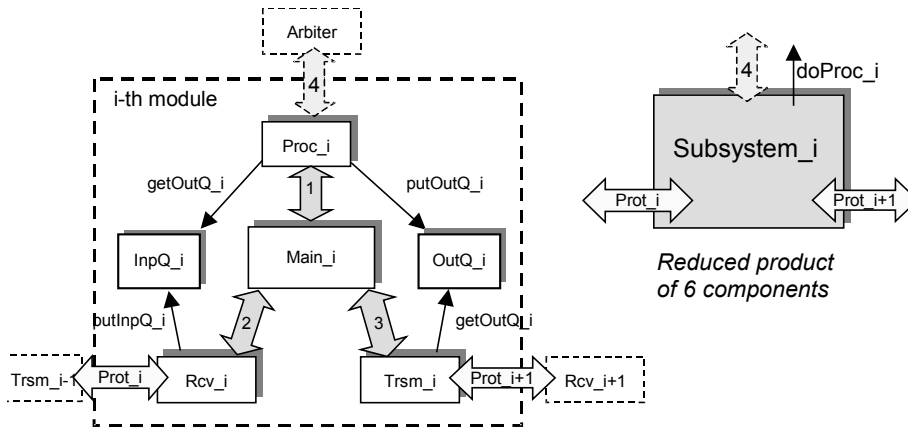


Fig. 2. 'Local' product of a single module

In order to obtain the 'phase-1' model of our example system we perform the following procedure:

Phase-1

1. Take a subsystem, consisting of the six components of module #1 (see Fig. 2),
2. Compute its CSM product,
3. Reduce it, leaving as the relevant output symbols the following ones:
 - All the output symbols (from the subsystem) which are 'watched for' by subsystem's communication partners (i.e. the *Arbiter*, *Trsm_0*, *Rcv_2*),
 - Symbols from the set selected above, which are produced within module #1 (this case: *doProc_1*),

Let the product reduced this way be called *Subsystem_1*,

4. Repeat the above for modules #2 and #3 obtaining *Subsystem_2* and *Subsystem_3* (respectively).
5. Substitute subsystems 1, 2, 3 in the place of just processed components.

This way we obtain the phase-1 structural model, in which subsystems 1, 2 and 3 are replaced by single automata. It is noteworthy that for *Subsystem_1*:

- Cartesian product of its six components has 24300 states,
- CSM product (before reduction) has 24 reachable states and 31 edges,
- After reduction, *Subsystem_1* is a graph of 10 states and 16 edges.

² Note that among the 'remaining components' can be also the additional, auxiliary automata (e.g. *Invariant*, in our case) necessary for expressing the properties under checking.

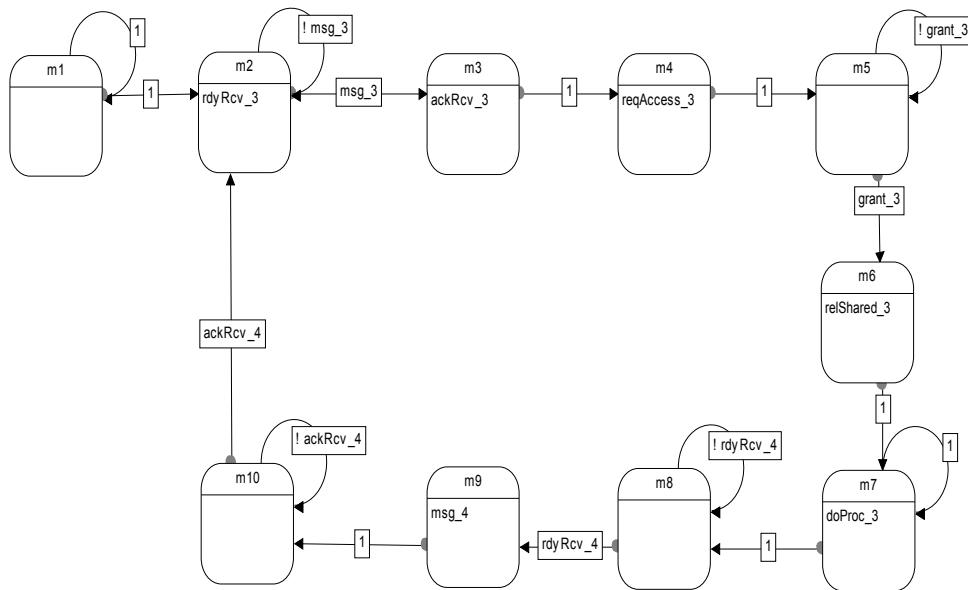


Fig. 3. CSM model of *Subsystem_3* (reduced product of six components of module #3)

For *Subsystem_3*, the situation is analogous. As an illustration, the reduced CSM product of six components making *Subsystem_3* (*Main_3*, *Rcv_3*, *Trsm_3*, *Proc_3*, *InpQ_3*, *OutQ_3*) is shown in Fig. 3. At no surprise, it has 10 states and 16 edges, same as *Subsystem_1*. For *Subsystem_2* (not shown), it is as few as 7 states and 12 edges.

Now, the analogous procedure can be applied again to the structural elements of the reduced model, for instance:

Phase-2

- The procedure is applied to a subsystem consisting of *Subsystem_1* and *Trsm_0*, preserving all the output symbols which are ‘watched for’ by the communication partners (i.e. *Arbiter* and *Subsystem_2*) and symbols needed for temporal formulas to be evaluated (this case: *doProc_1* and *msg_1*),
- and to a subsystem consisting of *Subsystem_3* and *Rcv_4*, preserving ‘watched for’ symbols (i.e. *Arbiter* and *Subsystem_2*) and symbols for model checking (this case: *doProc_3* and *msg_4*),
- finally substitute *Syst_1_Trsm_0* and *Syst_3_Rcv_4* in the place of just processed components.

This way we obtain the phase-2 structural model as in Fig. 4. Notice that the phase-2 system now consists of *four* components (instead of 21 components of phase-0 structural model), each of significantly reduced size. This ‘downsizing’ the model can be continued, but each time the reduction is performed a certain conditions have to be met [12] so that the reduction is not necessarily guaranteed. Nevertheless, in practice the degree of reduction can be substantial.

Let the CSM product of the system from Fig. 4 be called *New_System* and serve as the new behavioral model in which the temporal requirements are evaluated. *New_System*, obtained again with the COSMA Product Engine, has 323 states and 1406 edges and is expected to preserve at least these functional properties of the original, flat version which can be expressed in terms of symbols *msg_1*, *msg_4*, *doProc_1*, *doProc_2*, *doProc_3*.

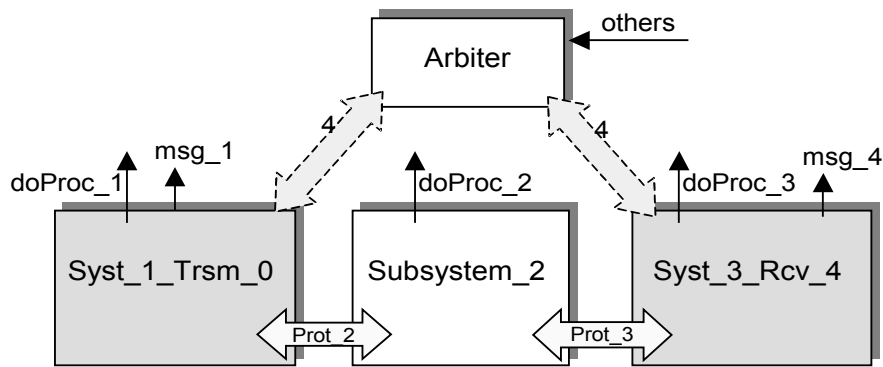


Fig. 4. Phase-2 structural model of the system

3 Verification of the reduced model

To sum up, now we have two behavioral models of the same example system:

- *Flat-product* (CSM product of 21 components, obtained as described in [1]) which had 8284 states and 34711 edges,
- *New_System*, obtained in the above two-phase reduction procedure, with 323 states, 1406 edges.

Both models have been verified in COSMA environment. As in [1], an additional automaton *Invariant* was determined to conveniently specify the verified properties. The checked properties were the following:

- Safety_1, saying – informally – that the number of messages within the pipeline never exceeds its capacity and the number of messages leaving the pipeline never exceeds the number of messages entering it,
- Liveness_1, saying – informally – that for any system state it is possible that the pipeline *eventually* would get empty,
- Liveness_2, saying – informally – that for any system state it is possible that the pipeline *eventually* would get full,

Experiments have been performed on PC computer with 800MHz processor and 512 MB RAM. Results are summarized in Table 1.

Notice that both formulas referring to the liveness have been evaluated *false* in both (flat and reduced) models. This negative result means that the system may enter such a state (states) that - from this state on - the pipeline is never empty again (i.e. it never terminates the processing of messages) or is never able to process three messages at once, which it was designed for.

The differences in evaluation times are really noteworthy: in all cases the ratio of $10^3 - 10^4$ in favor of reduced model was achieved, even though in terms of state space size the reduced model is only approximately 25 times less than the flat one.

Table 1. Summary of experiments

	Flat model		Reduced model	
	Result	Evaluation time	Result	Evaluation time
Safety 1	True	17 s.	true	< 1 ms
Liveness 1	False	54 s.	false	< 1 ms
Liveness 2	False	4 min 40 s.	false	60 ms

Finally, the model verification can be summarized as follows;

- The system itself performs wrong: there must be a synchronization bug in the specification of components. This calls for the analysis of a counterexample,
- The reduced model well preserves the relevant properties of the primary, flat one. Indeed, each case the same temporal formula was evaluated the same way (*true* or *false*) in both models,
- The multi-phase reduction method provides a significant gain in the evaluation time, even greater than the savings in the state space itself.
- The advantages of the evaluation algorithm used in the COSMA tool have been also confirmed. The algorithm terminates the evaluation as soon as the result (*true*, *false*) is certainly determined. It is why the evaluation times of rather similar formulas (1) and (2) differ by a few dozen of times.

4 Analysis of a counterexample

In the case of negative evaluation, the TempoRG checker [15, 17] produces a counterexample. Often, it is a path (a sequence of states) in the reachability graph that leads to the state where it was decided that the temporal formula is to be certainly evaluated false. In the case of more complex temporal formulas involving several operators, the counterexample can be a tree [15], showing which particular part of the formula (a sub-formula) is responsible for the negative result. Tracing the consecutive states along the counterexample, the designer is able to identify the synchronization bug.

However, in the case of *reduced* models, the model states can be unreadable. As a result of reduction, some states are eliminated, remaining ones are usually renamed etc., so that the analysis of counterexample should be based on the sequences of symbols (events) produced by the system instead of on sequences of states.

The evaluation of both formulas representing the liveness condition yields the same counterexample, presented in Fig. 5. The counterexample itself pretends to be a CSM, in order to enable the use of animation feature of COSMA tool. Using it, one can trace the states of individual components (and their change) corresponding to consecutive states of an counterexample. Also, some additional symbols (not used in ‘regular’ CSM) are also introduced as first elements of states’ output field. @ marks the starting state of the formula (this case it is system’s initial state) while F and G stand for operators of sub-formulas (*G* stands for **AG** and *F* stands for **AF**).

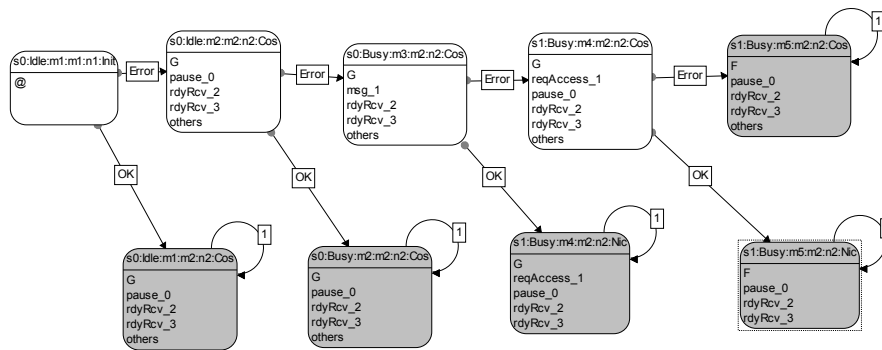


Fig. 5. Counterexample to the formula $AG AF$ in *Invariant.s3*

The counterexample is constructed as follows:

- it begins in the starting state of evaluation (the initial state in this example),
- it contains sub-paths responsible for sub-formulas (which may produce a tree-like counterexample),
- for four states two successors are shown: one which leads towards an erroneous state (in which the error is possible, transition labeled with *Error*), the other which leads to a ‘proper’ state (transition labeled with *OK*),
- the fifth state in an upper sequence, namely $s1:Busy:m5:m2:n2:Cos$ is referred to as a *Trap*. The rules of constructing counterexamples [24] say that this state is a representative of so-called Ending Strongly Connected Subgraph (ESCS) of states in which the most nested formula (*in Invariant.state*; $state \in \{s0, s3\}$) is not satisfied. When the system falls into one of these states, the error is inevitable (the desired state *state* of *Invariant* is never reached).

The *analysis* starts with finding the last one of states (in the sequence) that has two outgoing transitions: one labeled *OK* and the other labeled *Error*. This state is referred to as a *Checkpoint*. In the example, it is ($s1:Busy:m4:m2:n2:Cos$), with two successors: ($s1:Busy:m5:m2:n2:Nic$) as ‘proper’ state and

($s1:Busy:m5:m2:n2:Nic$) as a ‘wrong’ one. This time, the ‘wrong’ state is actually the *Trap* itself, but often it is only the initial state of a sequence of states which *inevitably* ends in a trap. Analysis of signals generated in the triangle {*Checkpoint*, its ‘proper’ successor, its ‘wrong’ successor} reveals the nature of error. We see that in the *Checkpoint* a request of access to the shared resource is generated (signal req_Access_1), and the resource is granted to another user (signal $others$ is present). For this state, its ‘proper’ successor does not produce $others$, while in the *Trap* the symbol $others$ is still present. So, *OK*-labeled transition (to a ‘proper’ state) is executed only if signal $others$ is withdrawn, otherwise the system chooses a transition to a ‘wrong’ state which leads to the *Trap*. In other words, the error is inevitable, if the request (req_Access_1) is issued while other users do use the shared resource.

Actually, in the system the two-state dead-end subgraph (causing a livelock of the whole system) can be found. System performs incorrectly because $reqAccess_1$ is not stored. Recall that in the CSM framework no implicit buffering of events is assumed: this should be provided by the model itself, e.g. by an additional (e.g. two-state) buffering component or by a simple modification of *Proc_1*. The same conclusion refers to the third module which accesses the shared resource as well. Both modules (#1 and #3) have been easily corrected and positively verified.

Finally, we may add that the flat product of the *corrected* system has 8086 states, 33588 edges instead of 8284 states and 34711 edges of the (incorrect) flat product discussed in [1]. This confirms the observation that the better the synchronization is, the less is the behavioral model of a system.

5 Real-time dependencies

Now we may convert automata to TSCM (Timed CSM, derived from CSM as Timed Automata [18, 19]) by adding time constraints and clock resets on some transitions in automata *Proc_i* and control units *Main_i* (Fig. 2). All time dependencies are shown as multiples of a basic time period, a *tick*. The constraints in *Proc_i* (Fig. 6) informs what is the minimal time of processing ($tim1$: by the constraint on the transition outgoing from the state *UseShared*) and the maximal time ($tim2$: the constraint on self-loop of the state *UseShared*). The constraints are based on a clock T_i local to *Proc_i*. The fixed time of staying in states in *Main_i* models delays in control unit. The clock is being reset every time the automaton enters *UseShared*. The constraints guarantee that the time of using a shared resource is finite. The constants $tim1_i$ and $tim2_i$, $tim1_i < tim2_i$, may be specific to subsystems 1,2 and 3. Auxiliary automaton which guarantees finite time of using the resource by $others$ must be modeled. Also, maximal time of a time period between generation of items should be specified.

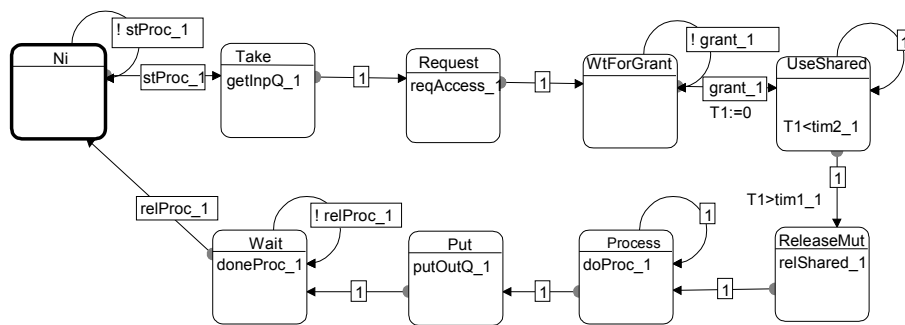


Fig. 6. Timed automaton *Proc_1*

Now we may convert automata to TSCM (Timed CSM, derived from CSM as Timed Automata [18, 19]) by adding time constraints and clock resets on some transitions in automata *Proc_i* and control units *Main_i* (Fig. 2). All time dependencies are shown as multiples of a basic time period, a *tick*. The constraints in *Proc_i* (Fig. 6) informs what is the minimal time of processing ($tim1$: by the constraint on the transition outgoing from the state *UseShared*) and the maximal time ($tim2$: the constraint on self-loop of the state *UseShared*). The constraints are based on a clock T_i local to *Proc_i*. The fixed time of staying in states in *Main_i* models delays in control unit. The clock is being reset every time the automaton enters *UseShared*. The constraints guarantee that the time of using a shared resource is finite. The constants $tim1_i$ and $tim2_i$, $tim1_i < tim2_i$, may be specific to subsystems 1,2 and 3.

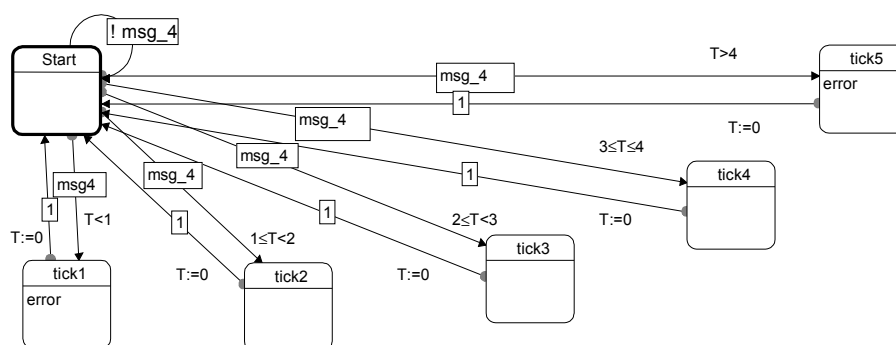


Fig.7. Testing timed automaton

Auxiliary automaton which guarantees finite time of using the resource by *others* must be modeled. Also, maximal time of a time period between generation of items should be specified. The model may be reduced as earlier, but in states subject to reduction their time constraints should match.

Now, the state space may be calculated following the rules given in [20], and RSCSM (Region automaton) may be constructed from product TSCSM (TSCSM does not specify the succession relation unambiguously). Basing on RSCSM state space, a testing automaton may be constructed, as shown in Fig. 7. This automaton checks if a time period between two items on output of the whole system is $\langle 0,1 \rangle$, $\langle 1,2 \rangle$, $\langle 2,3 \rangle$... ticks. If we impose a minimal and maximal time on the system, states violating the limits should produce the *error* signal (period $\langle 1 \rangle$ or $\langle 4 \rangle$ in this case).

The presented verification should be completed by a test using *invariant* automaton, because time constraints may change the behavior of the system.

6 Conclusions

The advantage of the formalism of Concurrent State Machines is that in order to understand (or even to design) the behavioral specification of a system component one has to be familiar with only a few elementary notions: a state, a transition, an atomic symbol, a Boolean formula, a time constraint. Generally, the semantics of an individual CSM is not far from the conventional finite state machines or basic UML's state diagram. However, given a collection of such CSM components, one can select a subsystem and obtain its product, representing (in one, large graph) all possible subsystem's executions or runs. Consequently, the model of a system can be subject to formal model checking methods and techniques. This advantage is not provided by a standard specification methods based on UML.

Moreover, as we have shown, the COSMA software environment supports the additional functional features, like stepwise model reduction, defining behavioral invariants, imposing time dependencies etc., as well as the means for the analysis of counterexamples. This makes the (Timed) Concurrent State Machines (and COSMA tool) a good candidate for a convenient framework for preliminary specification of concurrent, reactive systems. Once verified and corrected, such a specification can be refined, enhanced and otherwise developed in other professional software development environment. Moreover, if some components are to be *hardware*-implemented (which is often the case in embedded systems), the automata-like CSM specification is also close to common forms of behavioral specification of sequential circuits.

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